

7.1- Randomness

Random =

- * Individual outcomes are uncertain
- * Pattern/regular distribution in long run (lots of trials)

Ex: Coin flip, Roll 1 die, etc. , Plinko, Let's make a Deal

Probability =

- * describes how often the event occurs decimal/ %
- * between 0 and 1 (or 0 and 100%)

Simulation =

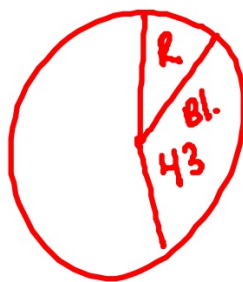
- * Using random digits (from a table, calculator, or computer) to imitate chance behavior
- * Let #'s = events
- * Generate #'s to represent events happening (perform an expt)

$\text{randInt}(0,1)$
 $(0,9)$

0-4 = right
5-9 = left

00-99

$\text{randInt}(1,6)$



$\text{randInt}(1,4)$
 $(1,12)$

Writing Instructions for a simulation:

- 1- Identify all outcomes & their probabilities
- 2- State your random number generator
(TRD or calculator)
- 3- Assign digits to represent all the outcomes.
- 4- State when you will stop one trial, and how many
total trials you will perform
- 5- State your response variable

Example: A baseball player gets a hit in 30% of his at-bats.
Simulate him coming to bat 12 times.

1) Identify the outcomes and their probabilities

Hit = 30%.

Not Hit = 70%.

2) Decide on your generator and assign the events to the generator

TRD Hit = 00-29 = 0-2 = 1-3

Not = 30-99 = 3-9 = 4-0

3) What is your response variable? Create a table to record

hits

Hit	Miss	line
	 	132

4) What is one trial? How many trials?

one at-bat

12 trials total

$$P(\text{hits}) = \frac{4}{13}$$
$$= 0.308$$
$$30.8\%$$

Example: Picking a card, and looking at the suit. Simulate 10 picks.

1) Identify the outcomes and their probabilities

Heart = 25% Spade = 25%

Diamond = 25% Club = 25%

2) Decide on your generator and assign the events to the generator

TRD

H = 00-24

S = 50-74

H = 1

D = 25-49

C = 75-99

D = 2

S = 3

3) What is your response variable? Create a table to record

C = 4

Suit
of
card

H		1
D		1
S		111
C		1111

Ignore 5-9, 0

4) What is one trial? How many trials?

one card pick

10 trials
total

Line
110

Example: A certain Stat class consists of 46% males. Simulate the teacher picking 8 students and recording their gender.

1) Identify the outcomes and their probabilities

Male 46%
Female 54%

2) Decide on your generator and assign the events to the generator

TRD $M = 00-45 = 54-99$
 $F = 46-99 = 00-53$

3) What is your response variable? Create a table to record

4) What is one trial? How many trials?

Example: A spinner has 4 sections: 50% Red, 13% Blue, 12% Green, 25% Yellow. Simulate spinning the spinner 20 times.

1) Identify the outcomes and their probabilities

2) Decide on your generator and assign the events

Red = 00-49 .

Blue = 50-62

Green = 63-74

Yellow = 75-99 .

Example: Back to the baseball player who gets a hit 30% of the time. Assume he gets on average 3 at-bats per game. Simulate 15 games, recording the number of hits per game.

1) Identify the outcomes and their probabilities

Hit = 30%.

Miss = 70%.

line 120

2) Decide on your generator and assign the events to the generator

TRD Hit = 0-2

Miss = 3-9

$P(H=3) = 0\%$

$P(H=1) = \frac{2}{8} =$

3) What is your response variable? Create a table to record

hits per game

# hits	frequency (#)
0	
1	
2	
3	

$\bar{X} =$

4) What is one trial? How many trials?

3 at-bats 15

Example: Back to the stat class... it consists of 46% males. A teacher needs to pick a group of ~~6~~⁴ students. What is the chance that she gets all 3 males? Simulate this 5 times to make your decision

1) Identify the outcomes and their probabilities

Male = 46%

Female = 54%

2) Decide on your generator and assign the events to the generator

TRD M = 00-45

F = 46-99

line
125

3) What is your response variable? Create a table to record

$P(X=3) = \frac{2}{5}$

males
in group

# M	frequency
0	
1	1
2	11
3	11
4	

$$\bar{x} = \frac{11}{5}$$

4) What is one trial? How many trials?

4 students

5 times

$$\bar{x} = 2.2$$

Use the table to complete the simulation

04592 32952 29485 23947 59602 18375 10395 10934 59606
 13487 23498 13284 23487 34857 21089 82973 42938 47589
 27459 84275 87647 62097 45872 48755 61324 90480 19438
 70648 75139 81457

# males	frequency
0	
1	1
2	
3	1
4	

Example: Picking a card, looking at the suit. We want to pick cards until we get a HEART. On average, how many cards will we need to pick? Do 5 trials.

1) Identify the outcomes and their probabilities

Heart = 25%. Heart 25%. Spade 25%.
Other = 75%. Diamond 25%. Club 25%.

2) Decide on your generator and assign the events to the generator

TRD Heart = 00-24 = 0,1 ignore 8,9
Other = 25-99 = 2-7

3) What is your response variable? Create a table to record

cards
until heart

5 trials
total

4) What is one trial? How many trials?

until get a heart

# cards	
1	
2	
3	
4	
5	
6	
7+	

Conduct the simulation $H=00-24$

10984 37576 41509 87140 98755 09671 92843 76098
 27435 09871 23875 09821 36458 20974 35098 21643
 98750 43275 98236 49726 59810 98473 19863 47563
 20497 25098 65276 81943 65726 43584 23460 27069
 81734 50961 09745 89174 39865 32498 67298 34657
 18643 75980 96424 08864 08862

$\bar{x} =$

# cards	freq
1	1
2	1
3	1
4	1111
5	

#cards	freq
6	
7	
8	
9	
10+	1 (25)

Try the Simulations Worksheet

#1)Instructions:

* Outcomes: Male = 50% Female = 50%

* TRD Female = 0 -- 4 Male = 5 -- 9

* 1 trial = having 3 children
total 10 trials

* Response Variable = # of girls

39634 62349 74088 | 65564 16379 19713 | 39153 69459

17986 24537 92740 92438 03957 14595 35050 40469

27478 44526 67331 93365 54526 22356 93208 02847

91374 15374

# G	freq	Exp. Prob.
0	1	10%.
1	111	50%.
2	111	30%.
3	1	10%.
10		

#2) Instructions:

- Outcomes : Girl = 50%
Boy = 50%
- TRD Girl = 0-4
Boy = 5-9
- one trial = until get a boy
Perform 10 trials
- Response Variable = # of children they have

39634	62349	74088	65564	16379	19713	39153	69459
2 1 3	4	1 3 1	1 1 1 1	3 2			
17986	24537	14595	35050	40469	27478	44526	67331
93365	54526	22356	93208	30734	71571	83722	79712
25775	65178	07763	82928	31131	30196	64628	89126

Girls = 0-4
 Boy = 5-9

1	111 1
2	1
3	11
4	1
5	

③ • outcomes = complete = 65%
incomplete = 35%

• TRD complete = 00-64
incomplete = 65-99

• one trial = 12 passes
perform 6 trials

• Response variable = #complete

80583 70361 41047 26792 78466 03395 17635 09697
 82447 31405 00209 90404 99457 72570 42194 49043
 24330 14939 09865 45906 30734 71571 83722 79712
 25775 65178 07763 82928 31131 30196 92347 60830

09230 47592 01832 05068 12838 12305 58506 37593

62941 17068

$$\bar{X} = \frac{48}{6} = 8$$

# Comp.	freq
7	111
8	1
9	1
10	1
11	

4) Instructions:

- * outcomes: catch = 78% miss = 22%
- * Use TRD catch = 00 -- 77 miss = 78 -- 99
- * One trial = 9 passes thrown to him
Perform 10 trials
- * Response variable = # catches

05409	20830	01911	60767	55248	79253	12317	84120
	7			6			
77772	50103	95836	22530	91785	80210	34361	52228
	7			7			
33869	94332	83868	61672	64628	89126	91254	24090
	7			4			
25752	03091	39411	73146	06089	15630	42831	95113
43511	42082	15140	34733	68076	18292	69486	80468
80583	70361	41047	26792	78466	03395	17635	09697
82447	31405						

$$\bar{x} = \frac{38}{6} = 6.33 \text{ catches}$$

#5)

outcomes: 6 different toys
all $\frac{1}{6}$

TRD each toy # 1-6
 ignore 7, 8, 9, 0

one trial = until we get one of
 each of 6 toys

Perform 10 trials

Response Var = # boxes opened

95836 22530 91785 80210 34361 52228 33869

94332 83868 61672 65358 70469 87149 89509

72176

5 5 3 6	22530	1 1 2 5 (13)	2 21 0	3 4 3 6 1	52228	33 3 6 9 (11)	4 4 3 3 2
3 3 6 6	616 1 2	65358	4 4 6 6	1 4 9	5 5 0 0 (10)	021 0 6	1 0 1 0 3/
5516 1	0 0 5 4	0 2 0 2	2 0 5 0 2 (16)	0224 0	0 4 3 1	361 0 2	4 0 221
1 4 1 1 (12)	5 343	6 0 5 1	4 0 4 5 (18)	55 0 6	1 0 6 4	416 1 2	4 0 5 1
3 3 5	4 0 134 (13)	34652	415 1	4 631	4 1 1 4 (12)	3 1 2 5	1 1 7 6
61 3 5	5 3 6	6 6 2 2	2 2 2 2	3 3 3 3 (20)	52 3 25	5 546 7	6 6 1 3
98072	91942	48917	48129	48624	48248	91465	54898